

"I have set my rainbow in the clouds"
we add: "and it shall be at 42° with
respect to you and the sun due
to refraction and geometry..."

Also
today : Creating light from darkness

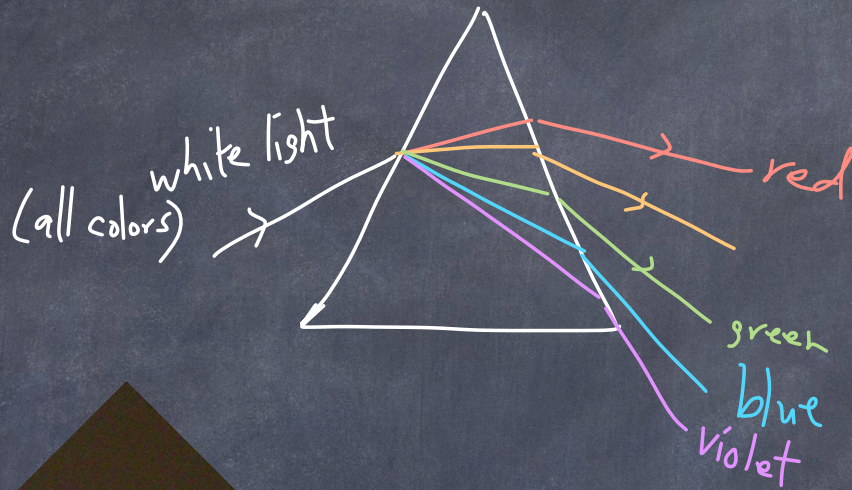
PHY 117 HS2023

Week 13, Lecture 1

Dec. 12th, 2023

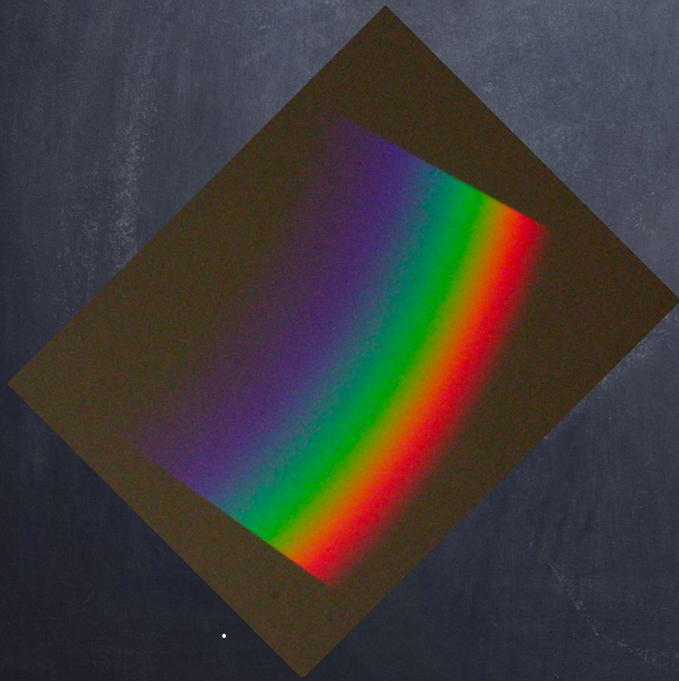
Prof. Ben Kilminster

In addition) The index of refraction, n , depends slightly on the wavelength of the light

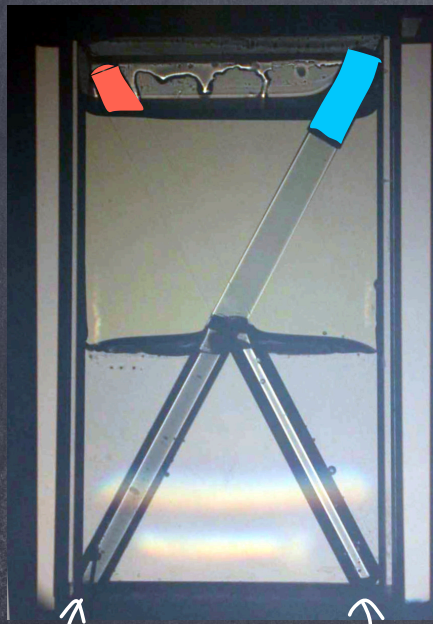


(exaggerated)

short wavelength
is bent more
blue bent more than red



$n_1 = n_2$ for one of the glasses



oil

water

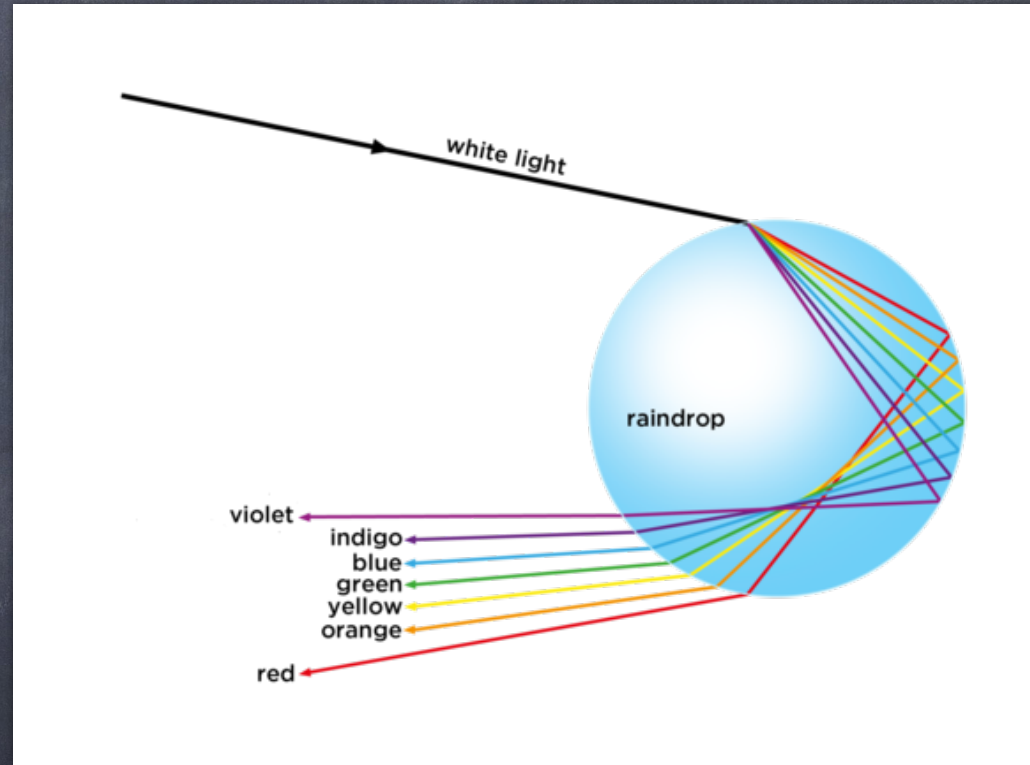
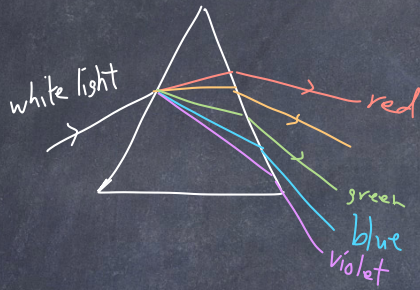
glass one

glass two

W 93

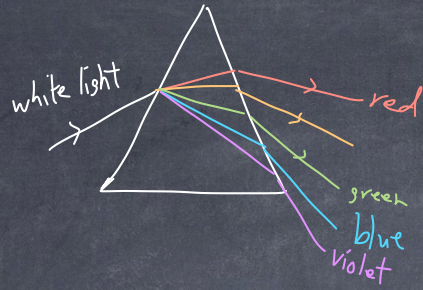
Farbe	Material	Brechungsindex
rot	Borsilikatglas (Pyrex)	1.473 (587.6nm)
blau	Weichglas (AR)	1.5 - 1.6
schwarz	Quarzglas	1.46
	Mandelöl	1.470 - 1.4715
	Wasser	1.33

Light through a rain drop



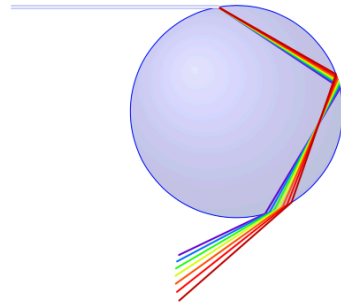
Light is refracted at different angles depending on λ

Pyramid!



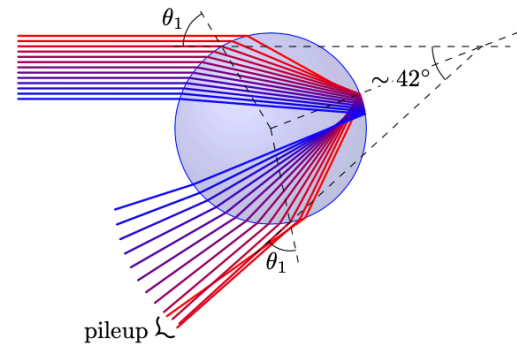
water droplet sphere!

Different wavelengths:



(a) A white light beam is spread in a rainbow due to dispersion (not to scale).

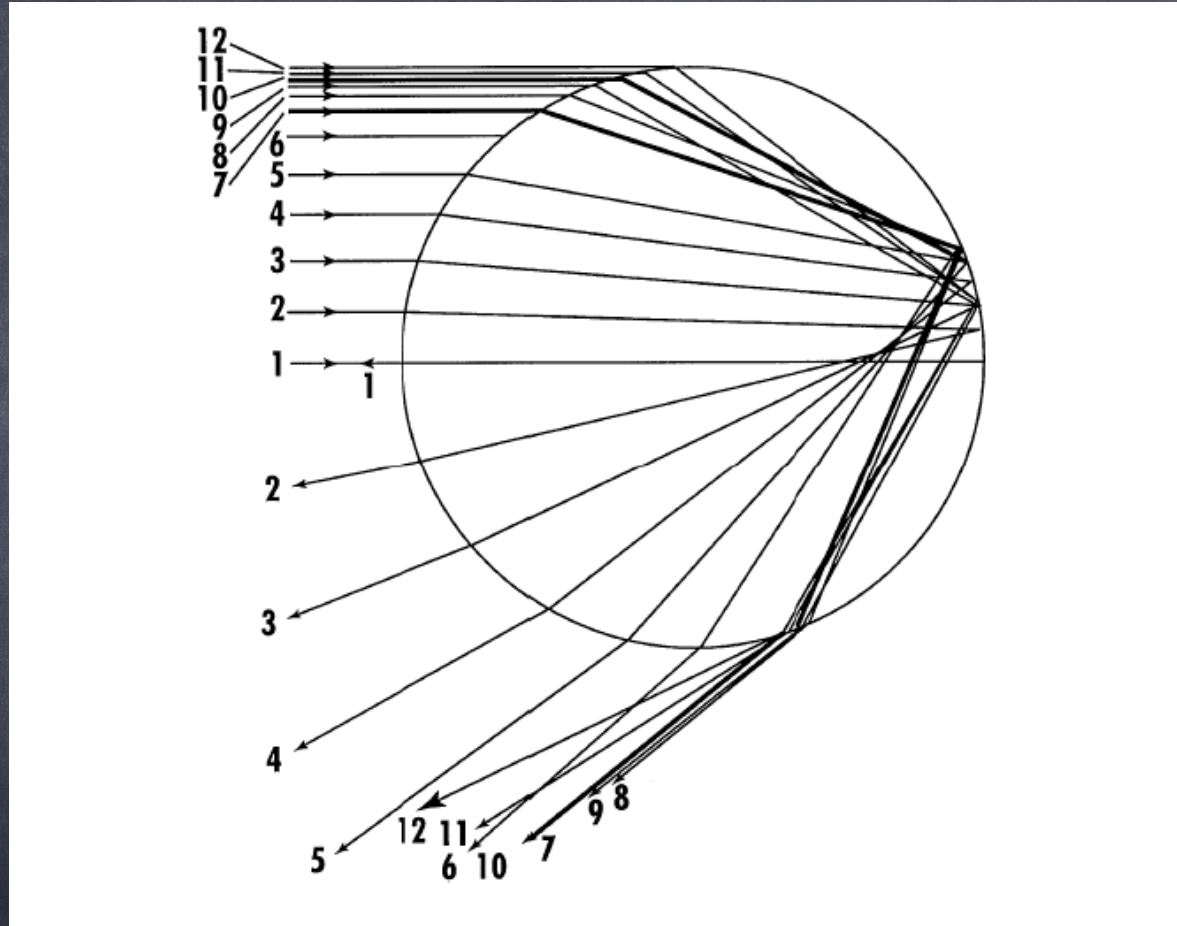
Same wavelength
Different paths



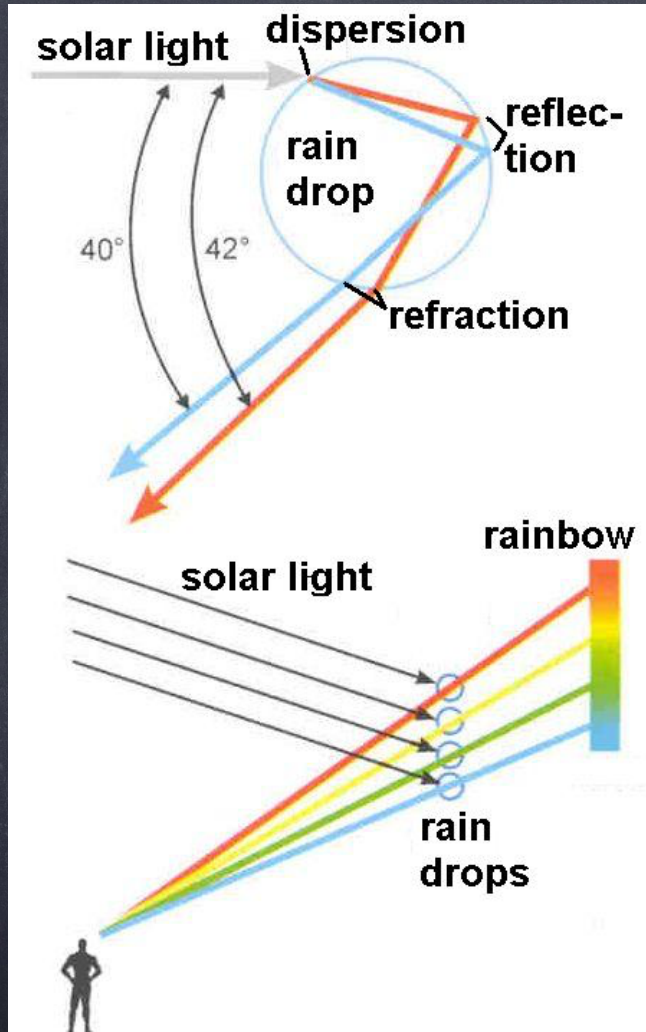
(b) At an effective reflection angle of about 42° , light is more concentrated (color unrelated to wavelength).

Figure 14.6: Explaining rainbows with dispersion and internal reflection in water droplets.

parallel
light
of same
wavelength
entering

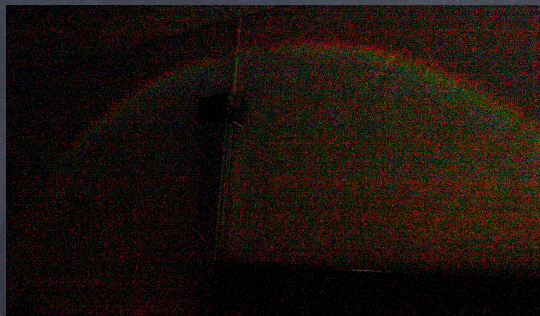


pileup of light
at a certain angle.

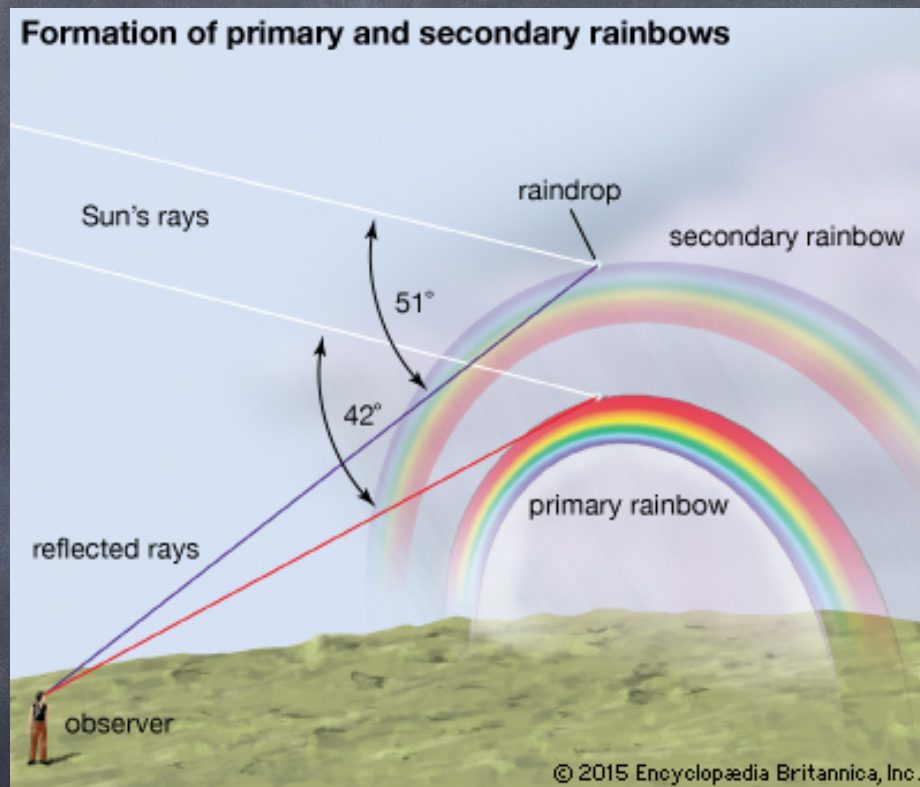
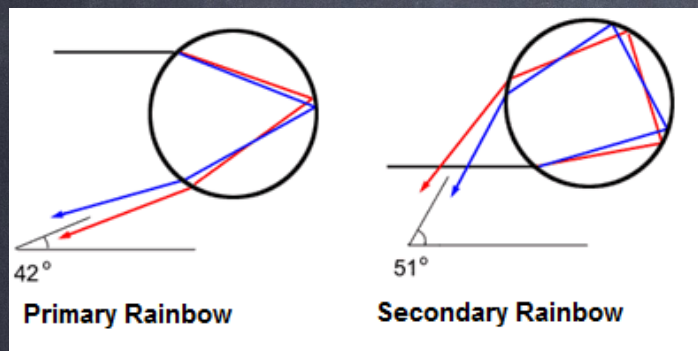


Blue light has an angle which piles up at 40°
and red light has an angle of 42°

This is how a rainbow works



Sometimes, you even see a second, "inverted" rainbow.



$\sim 42^\circ$



Look out for the second one!

Polarization - in any transverse wave

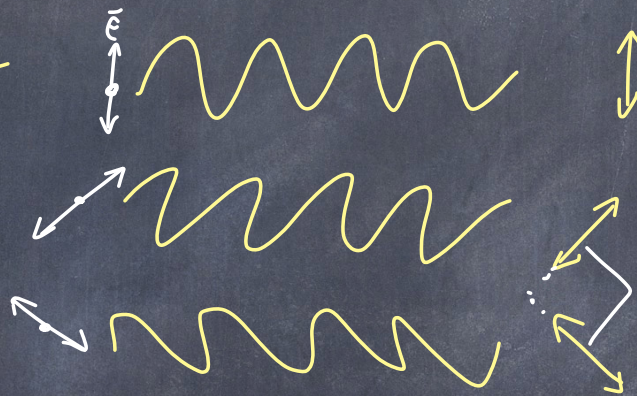
linear polarization

$\vec{E} \parallel$ to just one axis



unpolarized

many sources oscillating in random directions
(all $\vec{E} \perp$ to \vec{v})



combined



circular polarization

- \vec{E} rotates with time (* not in this class)

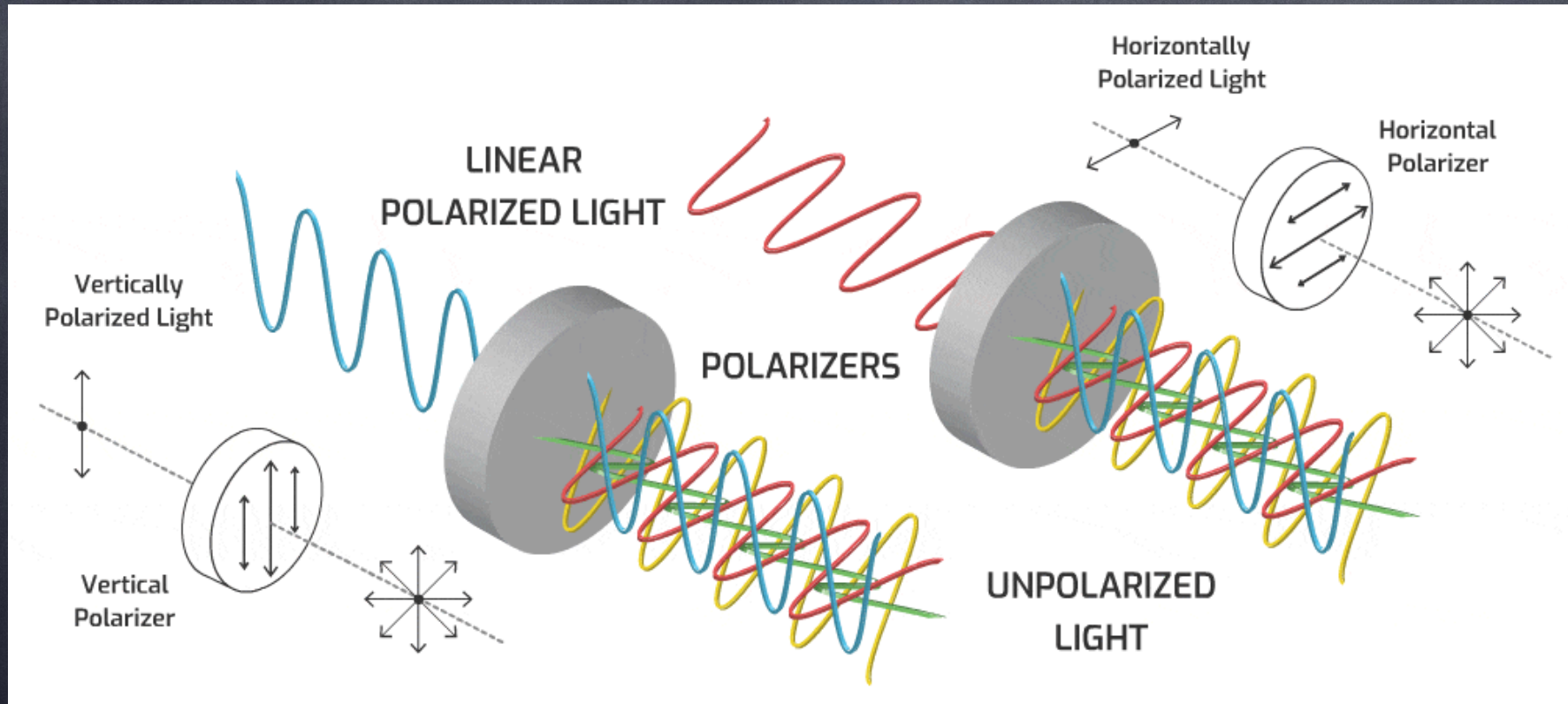
EM waves can be produced unpolarized in a substance since all atoms may act independently (random from heating) or polarized if coherent electric field

Polarized light can be produced from unpolarized light by:

- 1) absorption *
- 2) scattering
- 3) reflection †
- 4) birefringence

* In this class

absorption



polarizers can produce + detect polarized light

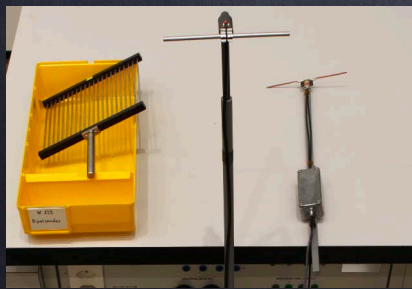
polarization by absorption:

When E -field is absorbed in one direction, then only the E -field \perp to the absorption is transmitted.

polarizing film or natural crystals

↑
long chains of hydrocarbons aligned, conducting at optical wavelengths.

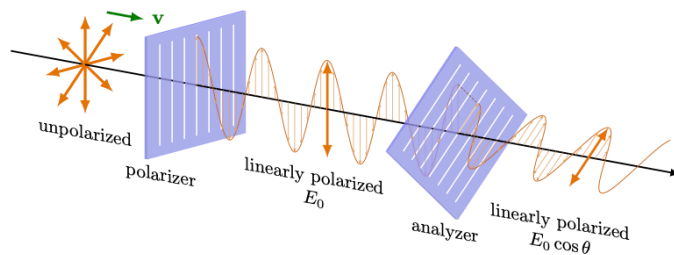
Example of microwaves



transmission axis is \perp to conductors

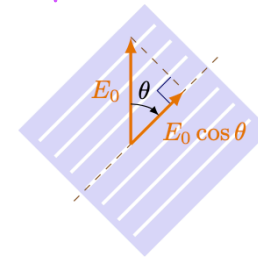
no light passes through

conductor parallel to \vec{E} absorbs polarized light



(a) Initially unpolarized light beam gets linearly polarized. The transmitted electric field is reduced to $E_0 \cos \theta$.

$$E_{\text{transmitted}} = E_0 \cos \theta$$



(b) Polarizer only lets through the component parallel to its polarizing axis.

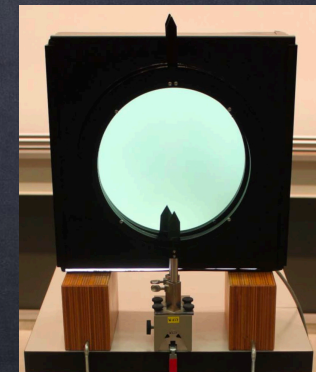
Two polarizing absorbers: polarizer, analyzer

The intensity of light goes like $|\vec{E}|^2$: $I \propto E^2$

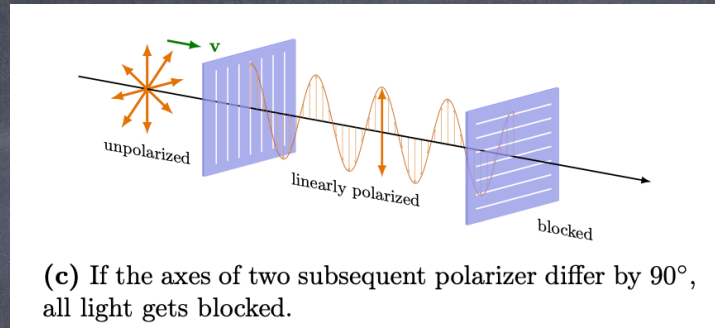
(electric field = E)

$$I = I_0 \cos^2 \theta \quad \text{Malus' Law}$$

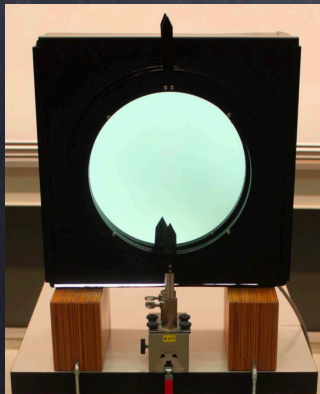
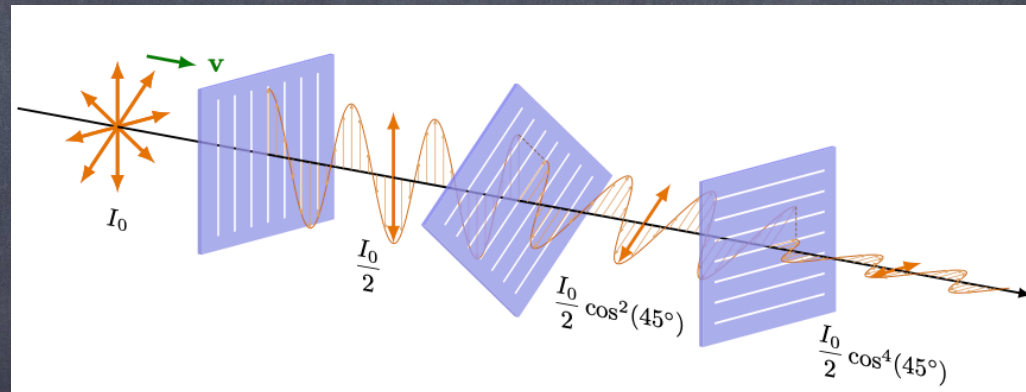
case! $\theta = 90^\circ \rightarrow I = 0$



No light passes



Light passes



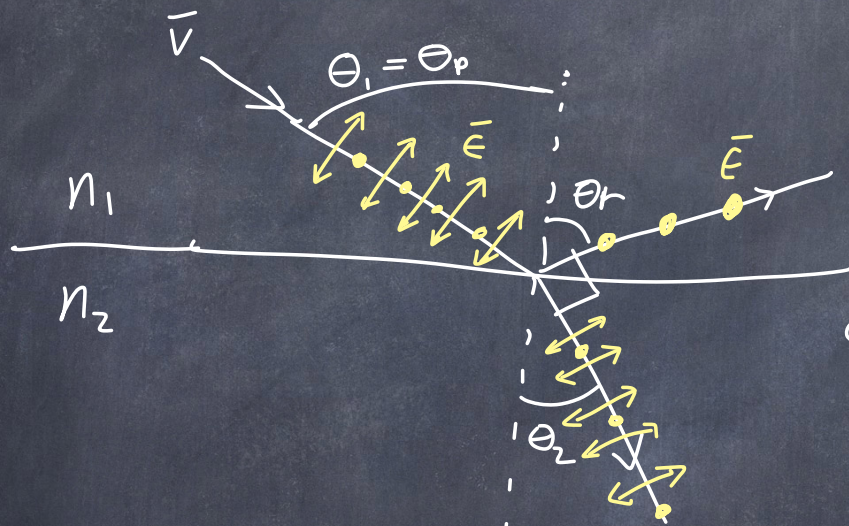
initial intermediate final

Example: $\theta = 10^\circ$
 $I_1 = I_0 \cos^2 10^\circ$

$\theta = 80^\circ$
 $I_2 = I_0 (\cos^2 10^\circ) (\cos^2 80^\circ)$

Polarization by reflection:

There is a partial polarization on the reflecting light reflected between two transparent media, such as air + glass, or air + water, ...



Incoming light as \vec{E} -field with 2 components, perpendicular to velocity

check: $\theta_r = \theta_i$
 $\theta_r + 90^\circ + \theta_2 = 180^\circ$

If the angle of incidence $\theta_i = \theta_p$ (polarization angle), which is defined such that there is a 90° angle between the reflected and refracted light, then the reflected light will be 100% polarized perpendicular to the plane of incidence.

The refracted light is slightly polarized.

condition of polarization by reflection:

$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

\updownarrow
 θ_p

The condition is that $\theta_2 = 90^\circ - \theta_1$

$$n_1 \sin \theta_p = n_2 \sin (90^\circ - \theta_p)$$

$$n_1 \sin \theta_p = n_2 \cos \theta_p$$

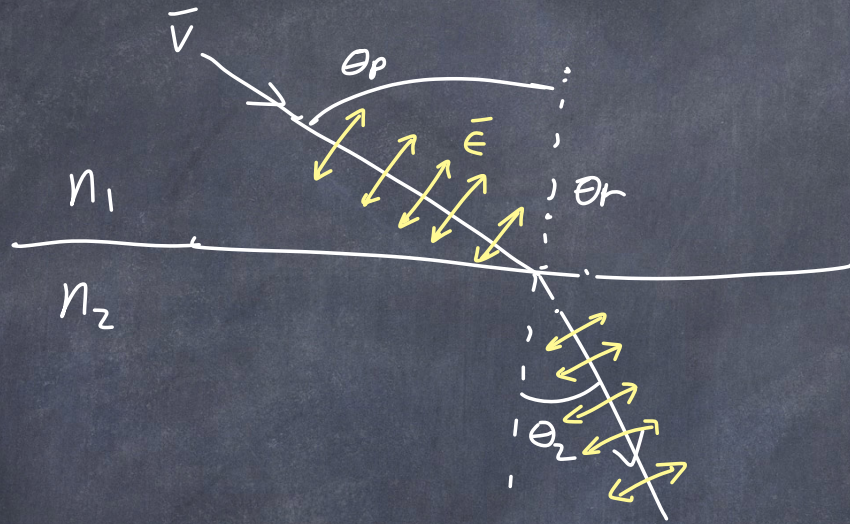
$$\tan \theta_p = \frac{n_2}{n_1}$$

Brewster's Law
for the angle of complete
polarization of reflected light

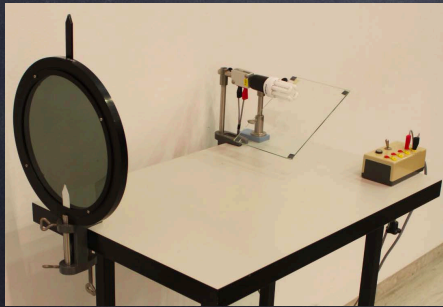
polarizer
used
as
analyzer



what if our initial light is polarized
in a direction \perp to surface
& direction of motion?

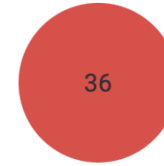


then at $\theta_i = \theta_p$,
no reflection
occurs



To calculate the B-field and E-field using Ampere's law and Gauss' law, one must define a closed surface.

1



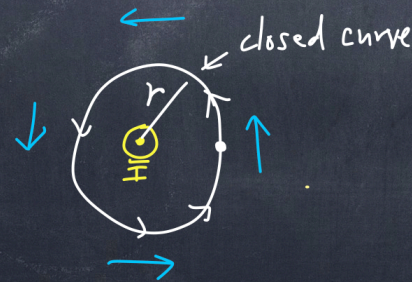
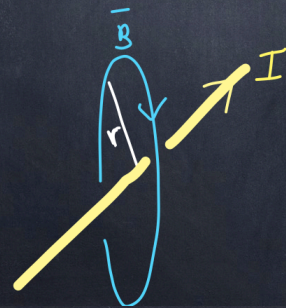
6

FALSE

Ampere's Law

$$\oint_{\text{closed curve}} \vec{B} \cdot d\vec{l} = \mu_0 I_c$$

I_c : current passing through the closed curve.



The sum of the voltages into a junction are the same as the sum leaving the junction.

1

24

18

FALSE

(iv) The sum of currents into a junction must equal the sum of currents out of the junction.

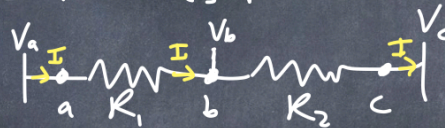
Current decreases when it moves through a resistor.

17

26

FALSE

Resistors in series:



Note: opposite rules
as for capacitors

Equivalent
resistance

$$R_{eq} = R_1 + R_2 + \dots$$

$$V_b = V_a - IR_1$$

$$V_c = V_a - IR_1 - IR_2$$

$$I_a = I_b = I_c = I$$

Potential decreases,
current stays
same.

A complete loop around any circuit will be equal to the battery voltage.

33

10

FALSE

(i) Any complete loop around a circuit has a total potential change of zero.
(Potential difference between 2 points is always the same, no matter which path)



↓

$$\text{Loop: } +\epsilon - IR = 0$$

$$IR = \epsilon$$

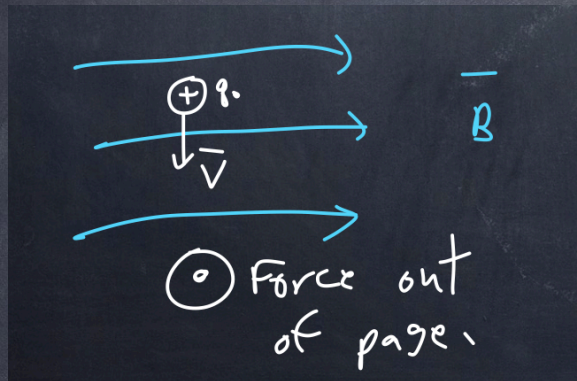
$$I = \frac{\epsilon}{R} = \frac{10V}{100\Omega} = 0.1A$$

Since a moving charged particle produces a magnetic field, the charged particle will feel a force from its own movement.

3

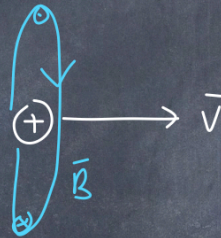
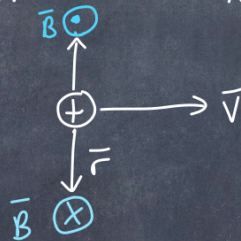
26

14



Now: A moving charge $\oplus \rightarrow \vec{v}$ generates its own magnetic field.

The direction of \vec{B} is $\vec{v} \times \vec{r}$



The magnetic field loops around the direction of motion.

The magnetic flux through 10 loops of optical fiber is 10 times more than through 1 loop.

3

17

23

Magnetic flux:

For a loop \perp to \vec{B} -field

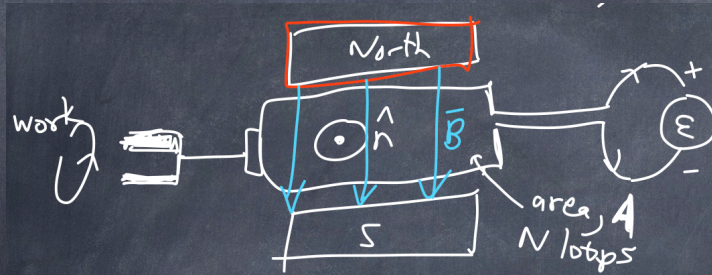
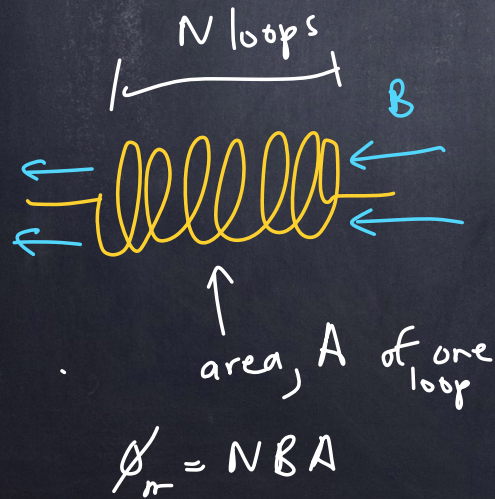


we can quantify the \vec{B} -field by

$$\Phi_m = BA$$

A: area

where Φ_m is known as the magnetic flux



magnetic flux through: $\Phi_m = NBA \cos \theta$
loop

$$\Phi_m = NBA$$

↑
of loops

7

A 4-sided loop of current, in which all 4 sides are perpendicular to a magnetic field, feels zero net force, but a non-zero net torque.

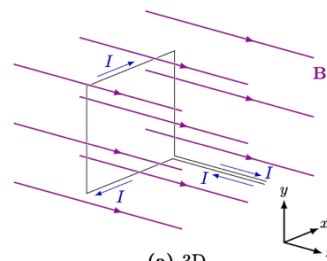
2

28

13

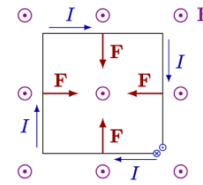
FALSE

80



(a) 3D.

CHAPTER 7. MAGNETISM



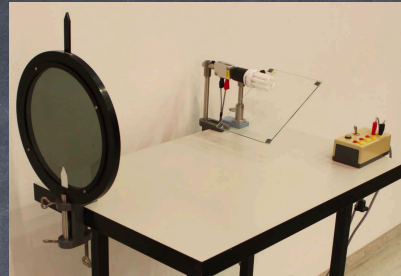
(b) 2D in xy plane.

Figure 7.9: Rectangular current loop in an external, uniform magnetic field $\mathbf{B} = B\hat{z}$.

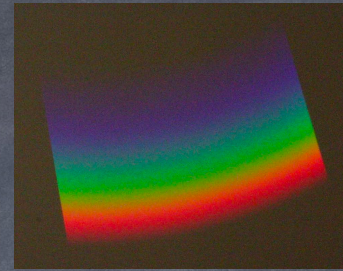
No net
force,
no net
torque



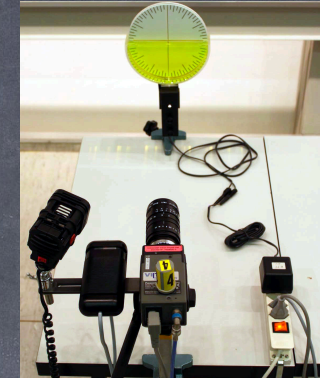
W51



W138



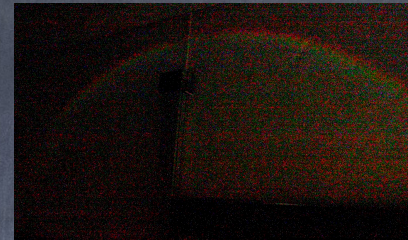
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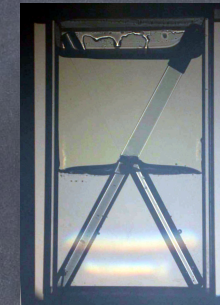
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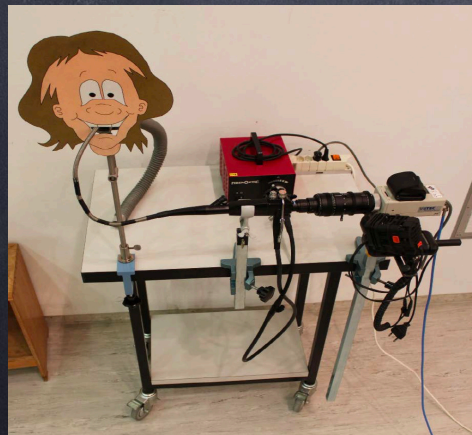
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W95



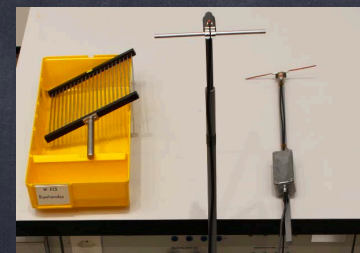
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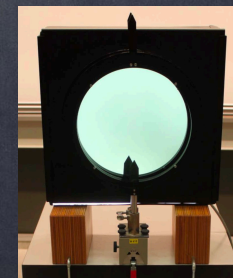
W78



W94



W139



W137